Optimum inhomogeneity of local lattice distortions in La₂CuO_{4+v}

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Electronic functionalities in materials from silicon to transition metal oxides are, to a large extent, controlled by defects and their relative arrangement. Outstanding examples are the oxides of copper, where defect order is correlated with their high superconducting transition temperatures. The oxygen defect order can be highly inhomogeneous, even in optimal superconducting samples, which raises the question of the nature of the sample regions where the order does not exist but which nonetheless form the "glue" binding the ordered regions together. Here we use scanning X-ray microdiffraction (with a beam 300 nm in diameter) to show that for La₂CuO_{4+v}, the glue regions contain incommensurate modulated local lattice distortions, whose spatial extent is most pronounced for the best superconducting samples. For an underdoped single crystal with mobile oxygen interstitials in the spacer La₂O_{2+v} layers intercalated between the CuO2 layers, the incommensurate modulated local lattice distortions form droplets anticorrelated with the ordered oxygen interstitials, and whose spatial extent is most pronounced for the best superconducting samples. In this simplest of high temperature superconductors, there are therefore not one, but two networks of ordered defects which can be tuned to achieve optimal superconductivity. For a given stoichiometry, the highest transition temperature is obtained when both the ordered oxygen and lattice defects form fractal patterns, as opposed to appearing in isolated spots. We speculate that the relationship between material complexity and superconducting transition temperature T_c is actually underpinned by a fundamental relation between T_c and the distribution of ordered defect networks supported by the materials.

granular superconductors \mid multiband superconductivity in density wave metals \mid scale-free heterogeneity \mid imaging phase separation \mid X-ray illumination

efects associated with lattice instabilities in solids are at the heart of many of their useful properties (1–3), including their electrical conductivity. For example, before the discovery of hightemperature superconductivity (HTS) in the cuprates, the search for new superconductors was influenced by the observation that the materials, such as Nb₃Al ($T_c = 19$ K), Nb₃Ga ($T_c = 20$ K), and Nb₃Ge ($T_c = 23$ K) (4), with the highest transition temperatures at the edge of structural instability. Since then, lattice instabilities have been proposed to favor HTS (5). Indeed, the search for electronic-lattice instabilities of local structure in copper oxides was a driving idea for the discovery of HTS in the pseudo-ternary oxide La_{2-x}Ba_xCuO₄ (6) and it was soon proposed that these materials were intrinsically phase separated (7). This was confirmed in La_2CuO_{4+y} , the simplest superconducting Cu oxide (with mobile oxygen interstitials) at the insulator to metal transition at very low doping (8). Further experiments also revealed different phase segregation in the optimum-doping regime (9). The key role of lattice complexity follows because the critical temperature in all known HTS superconductors increases in compounds made of an increasing number of atomic elements as shown in Fig. 1. The lattice complexity of superconducting copper oxides was neglected by most popular theories of high T_c superconductivity, while percolative theories for granular superconductors were invoked because of the relevance of lattice disorder for electronic properties (10).

Although surface defects, including their correlation with electronic properties, have long been investigated by surface-sensitive techniques such as scanning tunneling microscopy (11), bulk defect ordering has only recently become accessible. Here the important advance has been a novel experimental method taking advantage of synchrotron radiation focusing techniques: scanning X-ray microdiffraction. It has been used for imaging phase separation in the real space in cuprates, focusing on the selforganization of defects (12). A recent surprise has been that even for "optimal" samples in a single family, the ordering of oxygen interstitials is highly inhomogeneous (12). Nonetheless, while the best annealing protocol (13) in this instance did not yield homogeneous defect ordering, it did yield the most connected "fractal" network, thus suggesting that better superconductivity $(T_c = 40 \text{ K})$ is due to percolation of regions with the best ordering of interstitials. Defect growth and annealing processes, in fact, determine the quality of the superconductivity through either reduction of their population or complex self-organization (14, 15). The unanswered question concerns the nature of the medium hosting the regions with ordered interstitials. This is significant, as it will play a key role in determining many generic properties, from mechanical and chemical stability to the electrical characteristics, both in the superconducting and normal states of many cuprates that do show the ordering of mobile interstitials and other defects during sample preparation. An example of such a property is the often-observed linear relation between electrical resistivity and temperature, which could have an intrinsic, exotic origin in many-body physics but could also be specific to an inhomogeneous mixture.

For many years the dominant theories of HTS have considered a stoichiometric CuO₂ layer and have neglected the key role

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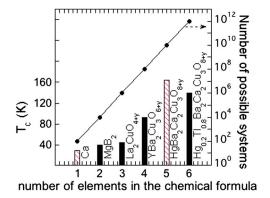


Fig. 1. The maximum superconducting critical temperature, discovered so far by material research, increases by increasing the lattice complexity. The maximum critical temperature at ambient pressure (sold bars) and high pressure (dashed bars) in systems made by a single element (Ca under pressure) and two elements (magnesium diboride) and copper oxides with multiple elements in the chemical formula.

of lattice effects (16, 17), even if the $[CuO_2]_{\infty}$ layers are intercalated by a variety of defective oxide AO layers (A=La, Ba, Sr, Ca, Y, Hg or Rare earths) with a large tolerance factor (18) or misfit strain (19, 20) and a large number of oxygen interstitials or defects. The lattice misfit induces tilting and corrugation of the $[CuO_2]_{\infty}$ layers and structural phase transitions going from I4/mmm (high temperature tetragonal), Bmab, Pccn, and Fmmm (low temperature orthorhombic, LTO) to P42/ncm (low temperature tetragonal) in systems like La₂CuO₄ (21).

Lattice effects, also leading to inhomogeneous internal strains in perovskite manganites with fixed hole concentrations, are well established and have been connected with their colossal magnetoresistance (22-24). It is therefore worth asking whether strain inhomogeneities are also an important feature of cuprates, where they could lead to apparent phase segregation (23, 24), inducing peculiar transport properties where the self-organization associated with long-range strain interactions could even induce electronic granular networks (25). Our recent discovery (12) that better superconductivity appears with "optimal inhomogeneity" (26) of oxygen defect (Oi) ordering opens the question of the nature of the remaining disordered medium, the topic of the present paper. The separation into an ordered network and a strained embedding medium provides a basis for the two electronic components (27-29) which have been proposed as the key feature for certain theories of high temperature superconductivity (30–32).

The local lattice distortions of the CuO₂ planes (33–37) provide another kind of ordered defect. In several doped cuprates, they yield a characteristic incommensurate superstructure with the specific wavevector 0.21b* (38-46). Recent scanning tunneling microscopy work has clearly shown that the local lattice distortions of the CuO₂ plane induce a spatial modulation of the gap (11). The incommensurately modulated local lattice distortions (LLD) are a type of static charge density wave (CDW) established in nanoscale regions, whose size is indicated by the widths of diffuse X-ray satellites (37–45). Here we use X-ray microscopy to show that for the cuprate superconductor, La₂CuO_{4+v}, the dominant features of the embedding glue regions, where interstitials are disordered, are optimally ordered arrays of tilt defects of the

copper-centered oxygen plaquets, which are the fundamental building blocks of the cuprates.

Materials

 $\mathrm{La_2CuO}_{4+\nu}$ is the simplest cuprate and therefore represents an ideal venue for investigation of LLD droplets. For 0.01 < y < 0.055, La_2CuO_{4+v} shows macroscopic phase separation between the y1 = 0.01 antiferromagnetic phase and the y2 = 0.055 superconducting phase (8, 41), where the sample shows the coexistence of two c-axis lattice constants corresponding to two competing macroscopic phases. For y > 0.055, La₂CuO_{4+y} shows more subtle phase separation, characterized by coexistence of two different superconducting phases with different critical temperatures, the first $T_{c1}=15\pm1~\text{K}$ and the second T_{c2} ranging between 27 and 38 K, even while the crystalline lattice shows no splitting of the c-axis. The first critical temperature is sensitive to Oi ordering, and the second critical temperature is similar to that seen for La_{2-x}Sr_xCuO₄ (11, 46, 47).

We first investigated the competition among Oi puddles and LLD droplets (see Table 1 for the acronyms) using a La_2CuO_{4+y} single crystal in the underdoped regime with y = 0.06, which corresponds to an electronic doping of 0.1 holes per Cu site. The superconducting critical temperature and the pinning properties have been characterized by ac-susceptibility experiments. The sample shows electronic phase separation into two superconducting phases with two critical temperatures, $T_{c1}=14\,$ K and $T_{c2}=27\,$ K (see Fig. S1), in agreement with previous studies (12, 47, 48). Synchrotron X-ray diffraction (XRD), performed at the European Synchrotron Radiation Facility (ESRF) at Grenoble, shows weak incommensurate diffuse satellites (called Q3-LLD) displaced by incommensurate wave-vector $\mathbf{q3} = 0.21 \, \mathbf{b} * +0.29 \, \mathbf{c*}$ from the principal Fmmm lattice reflections (see Fig. S2) for this mono-crystal. The diffuse weak Q3-LLD satellites coexist with Q2-Oi satellites (displaced by q2 = 0.25 $\mathbf{b}*+0.5$ **c***) due to O*i* sitting at the (¼, ¼, ¼) interstitial site position (49). Q3-LLD satellites dominate and are easier to detect in underdoped samples. On the contrary, Q2-Oi satellites are dominant at the optimum doping, for y > 0.1.

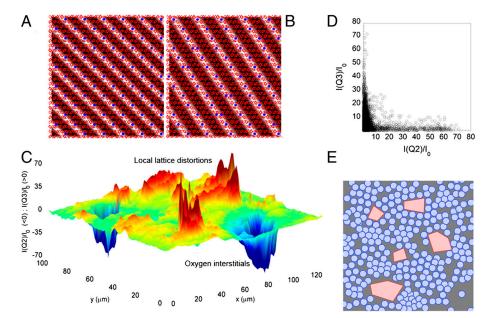
Results and Discussion

For our scanning X-ray microdiffraction experiments, we used the ID13 beam line of ESRF, optimized to deliver X-rays with an energy of 14 keV, focused on a 300 nm spot on the sample surface. Data were collected in the reflection geometry with a two-dimensional Fast Readout Low Noise Charged Coupled Device (FReLoN CCD) detector. We constructed images from 6370 XRD diffraction patterns, each one for a different spatial x–y position of the sample.

Fig. 2A and B contain schematics of the two coexisting structural modulations in the bc plane; the Q2-Oi and Q3-LLD respectively. Fig. 2C is a 3D image of Oi puddles and LLD droplets. We may recognize the isolated puddles (cold color) and the dominant droplets phase (hot color). Fig. 2D demonstrates that the two signals are anticorrelated. The results show that the ordered oxygen interstitials give a granular superconducting phase with $T_{c1} = 14 \text{ K}$ in the underdoped regime competing with the second superconducting phase made of a distribution of droplets of LLD with $T_{c2} = 27$ K. Fig. 2E shows a pictorial scheme of the spatial distribution of the LLD droplets (blue circles) with a 23 nm size, deduced from the diffraction line-width (see Fig. S2), and of the large Oi puddles (red polygons). The imaging of mesoscopic spatial inhomogeneity points clearly toward the assignment of the superconducting phases in La₂CuO_{4+v} with $T_{c11} = 14$ K in this sample and with $T_{c12} = 40$ K in the optimum doped sample (10) to the ordering of mobile Oi forming isolated puddles and their scale-free pattern organization respectively.

Table 1. Acronyms

Acronyms	
Oi Q2-Oi LLD O3-LLD	Oxygen interstitials sitting at the sitting at the ($\frac{1}{4}$, $\frac{1}{4}$) interstitial site position in the K ₂ NiF ₄ lattice structure Self organization of oxygen interstitials with superlattice wave-vector $\mathbf{q2} = 0.25 \mathbf{b} * + 0.5 \mathbf{c} *$ Local Lattice distortions Self organization of local lattice distortions with superlattice wave-vector $\mathbf{q3} = 0.21 \mathbf{b} * + 0.29 \mathbf{c} *$



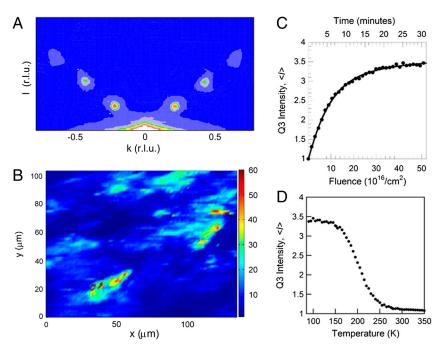


Fig. 3. (A) The CCD image of the Q3-LLD satellite in the b*-c* plane near the main Fmmm reflections of the underdoped La₂CuO_{4+y} single crystal, after the removal of the Q2-O*i* satellite by rapid quenching after heating the sample above 350 K. Crystals are cooled to liquid nitrogen temperatures (as low as 85 K) with a 700 series Oxford Cryosystems cryocooler. (B) The position dependence of the Q3-LLD superstructure intensity $I(Q3)/I_0$ in the 2D color plots after the removal of the Q2-O*i* superstructure intensity $I(Q2)/I_0$, by thermal annealing. (C) The intensity of the Q3-LLD XRD reflections is plotted as function of fluence ϕ or time for constant X-ray flux. The surface is illuminated by a X-ray flux $\phi_{P(0.1 \text{ nm})} = 5.10^{14} N_P \cdot \text{s}^{-1} \text{ cm}^{-2}$ keeping the temperature constant at 85 K. (D) The temperature evolution of the Q3-LLD satellite intensity in the range of 85 to 350 K collecting images every 2 K. The time evolution experiment has been carried out at the Elettra storage ring in Trieste. The X-ray beam, emitted by the wiggler source, was monochromatized at the 0.1 nm wavelength by a Si(111) double crystal monochromator and focused on the sample surface at the X-ray diffraction beamline (XRD1).

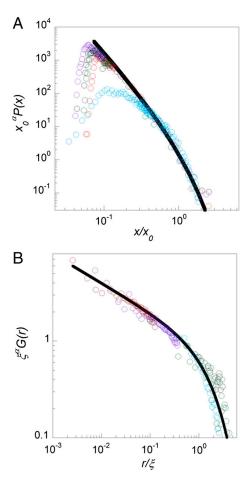


Fig. 4. (A) The probability distributions, P(x), of the Q3-LLD XRD intensity $x = I(Q3)/I_0$ for single crystals of electrochemically doped La₂CuO_{4+y} from the underdoped state (y = 0.06) to the optimum doping range, 0.1 < y < 0.12. The curves follow a power law distribution $P(x) \propto x^{-\alpha} \exp(-x/x_0)$ with a variable exponential cut-off x_0 . The curves $x_0^{\alpha}P(x)$ of all samples as a function of x/x_0 collapse on the same curve. (B) The spatial correlation function, G(r), of the Q3-LLD XRD follows a power law distribution $G(r) \propto r^{-\eta} \exp(-r/\xi)$. The correlation length ξ varies from 30 to 140 μ m increasing with the doping range of the material investigated. The curves $\xi^{\alpha}G(r)$ of all samples as a function of r/ξ collapse onto the same curve.

We have been able to obtain a sample showing only Q3-LLD satellites by disordering the Oi via heat treatments (11, 12) as shown in Fig. 3. We increased the sample temperature above the Oi order-to-disorder temperature—i.e., 350 K—followed by a rapid quench below 200 K. In such a way, Oi remains frozen in a disordered state and the Q2-Oi diffraction peaks, as measured by the CCD area detector, are completely missing (Fig. 3A). Fig. 3B is the scanning X-ray microdiffraction image of the pattern of LLD droplets in this sample with $T_{c2} = 27$ K.

To identify how LLD droplets can arise, we carried out experiments of photo-induced effects at the Trieste synchrotron radiation facility Elettra (13). The X-ray beam spot size was 200 µm² on the sample surface, and the flux (defined as the number of photons hitting the sample surface per second per unit area) $\Phi_{P(0.1~\mathrm{nm})}=5\times10^{14}\,N_{P(0.1~\mathrm{nm})}s^{-1}\,\mathrm{cm}^{-2}$ corresponds to a power density of 1 W cm $^{-2}$ on the sample surface. The X-ray photon beam is at the same time a pump and probe excitation of a surface layer of about 1.5 µm. The effect of continuous illumination corresponds to photoexcitation in which the state-changing rate is proportional to the intensity of the radiation. Therefore, the physical state of the system is controlled by the fluence $F_{P(0.1 \text{ nm})}(N_{P(0.1 \text{ nm})} \cdot \text{cm}^{-2}) = \Phi_P \cdot t$. The sample was kept at

constant temperature T = 85 K where the Oi are frozen (12, 13) in the disordered glassy phase of the quenched sample. Fig. 3C shows the time evolution of the intensity of the Q3-LLD satellites recorded in the CCD area detector probing the (b*c*)reciprocal space at the fixed temperature of 85 K. The time evolution of the Q3-LLD XRD intensity follows the equation $I(t) \propto (1 - e^{-\frac{t}{\tau}}) \cdot t^{\gamma}$. During experiments we checked that upon doubling or halving the flux, the timescales were halved or doubled, respectively; therefore the variation of the Q3-LLD intensity is plotted as a function of the fluence. The power-law regime for the droplets follows the increase of the XRD diffraction intensity, without threshold, with an exponent $\gamma =$ 0.1 ± 0.02 . To determine the temperature range where the X-ray illumination stimulates the Q3-LLD ordering, we have performed a thermal cycle from 100 K to 400 K under a high flux illumination. The Q3-LLD satellite intensity as a function of the temperature obtained by heating the sample after the X-ray illumination at 85 K is shown in Fig. 3D. The number of ordered domains Q3-LLD, proportional to the integrated intensity of the reflections Q3-LLD, returns to its initial value after increasing the temperature above 200 K. The results are in agreement with i) photo-annealing of the incommensurate modulated local lattice distortions detected by electron diffraction peaks below 200 K (43); ii) the photoinduced variation of superconducting properties (50, 51); and iii) with the onset of LLD below 200 K as detected by EXAFS (45).

The LLD droplets form networks whose nature varies with superconducting critical temperature. We have used X-ray microdiffraction apparatus at the ESRF to map the evolution of the Q3-LLD satellites for five single crystals of electrochemically doped La_2CuO_{4+y} , from the underdoped state (y = 0.06) to the optimum doping range, 0.1 < y < 0.12. Fig. 4A and B shows respectively the probability distribution of XRD Q3-LLD intensities and the spatial correlation function, G(r), where r = $|\mathbf{R}_i - \mathbf{R}_i|$, calculated for the intensities at the spots \mathbf{R}_k . From the XRD mapping we have extracted the probability distribution, P(x), of the intensity I(Q3) of the reflections due to XRD Q3-LLD satellites of the main crystalline reflections, and normalized to the background, $I(Q3)/I_0$. Normalized data have been divided by the mean XRD intensity of the sample, x, and scaled using a power law with a cut-off x_0 : $P(x) \propto x^{-\alpha} \exp(-x/x_0)$ with the power-law exponent $\alpha = 2.6 \pm 0.1$. All probability distributions of XRD intensities scale with the same power-law exponent α and a variable cutoff in the range from 4.5 to 15 (Fig. 4A). The spatial correlation function follows a power law, $G(r) \propto r^{-\eta} \exp(-r/\xi)$, with the exponent $\eta = 0.3 \pm 0.1$ and the correlation length $\xi = 30 \pm 10 \ \mu \text{m}$ in the underdoped y = 0.06 sample with $T_c = 27 \text{ K}.$

Looking at the distance-dependent intensity correlations from the underdoped to the optimum doping state indicates that the droplets self-organize in a fractal state. Fractals appear in many fields (52, 53), including all branches of materials science where new phases grow via stochastic nucleation and accretion at firstorder phase transitions (54). Of course the detailed nature, including characteristic exponents, will depend strongly on the details, such as annealing protocols and strain interactions, for the particular system under consideration. For the LLD regions in La₂CuO_{4+v}, the correlation length follows a power law with an exponential cutoff which progressively grows with higher critical temperatures. Fig. 4B shows that G(r) for samples with T_c in the range 27 K > T_c > 38 K collapse onto the same curve when plotted versus r/ξ . In particular, for 30 < T_c < 35 K, ξ is in the range of 40 to 120 μ m and for $T_c = 37$ 1 K it is 140 ± 20 μ m. At the same doping level, therefore, there are shorter correlation lengths for the LLD droplets than the Oi puddles, which in the optimal case can reach even 400 µm (12, 13).

Fig. 5 shows the T_c in the range 27–38 K, measured by complex resistivity (see Figs. S3 and S4), associated with the droplet net-

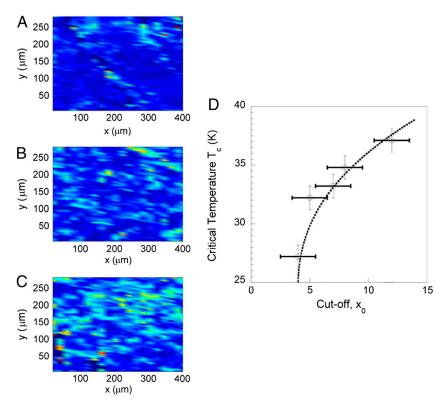


Fig. 5. (A, B, C) X-ray microdiffraction results for the position dependence of the Q3-LLD superstructure intensity $I(Q3)/I_0$ in the La₂CuO_{4+y} crystals with different critical temperature, T_c , 32, 34, and 37 K from A to C. The scanning XRD images show the better self organization of LLD droplets, proceeding to the higher T_c . D. The critical temperature T_c in the range 25 K < T_c < 37 K for five samples is plotted as a function of the cut-off parameter of the distribution of the LLD droplets density probed by the intensity distribution of the Q3-LLD superstructure satellites. Error bars in the critical temperature are of ± 1 K. The dashed line is the fit with a power law curve with exponent 0.4 ± 0.05 , in agreement with theoretical predictions (56) for granular superconductivity on a scale invariant network.

work, as a function of the cutoff of the probability distribution of XRD Q3-LLD intensities. The critical temperature scales with the cutoff according to a power law with an exponent 0.4 ± 0.05 . This result points again toward the importance of connectivity and an optimum inhomogeneity for high critical temperature (12, 26). It is also in qualitative agreement with the theoretical prediction of the increase of T_c in a granular superconductor on an annealed complex network with a finite cutoff (55, 56). In fact, for a power-law distribution of links in a granular superconductor with an exponent $\alpha=2.6$ the critical temperature is predicted to increase as a function of the cutoff with an exponent $3-\alpha$, as observed experimentally.

Conclusions

We demonstrate that $\text{La}_2\text{CuO}_{4+y}$ actually contains networks of two superconductors characterized by different ordered defects (Oi and LLD). The best fractal behavior and superconductivity is obtained simultaneously for both Oi and LLD order. In particular, we have provided a positive correlation between the cutoff, x_o , for scale-invariance of the LLD diffraction intensity distribution and T_c . Furthermore, the strains in the LLD droplets are correlated over the longest distances when the stresses produced over still larger distances by the ordered interstitials display their maximal correlations, a condition which also yields superconductivity with a maximum T_c . Therefore we argue that the best fractal Oi network strains the embedding medium with LLD order the most.

Our quantitative results should be tested against theories of composite, granular superconductors proposed for cuprates (10, 14, 15, 25, 30–32, 55–62). The X-ray data indicate that these theories must take into account not only the usual superconducting proximity effects, but also the effects of the strains the two com-

ponents exert on each other. It is the latter which must be ultimately responsible for the exponents α and η which we observe, and given the long-range nature of strain interactions, they cannot be accounted for within a simple near-neighbor percolation model. Our work provides a rationale for the observation of Fig. 1 showing that the main determinant of T_c is complexity of the underlying material. Indeed, having already shown that there are at least two highly relevant, coexisting networks of ordered defects in the simplest cuprate, it is quite possible that there are numbers N > 2 of such networks for the more complex materials. T_c then grows with N because of two effects: (i) the larger chances of optimal strain and Josephson (proximity) couplings with increasing N, even though the underlying nanoscale pairing propensities remain invariant, and (ii) the accommodation of larger doping densities in portions of samples with larger N. Our thinking suggests a clear program for future theory, taking into account random network, long-range strain and granular superconductivity concepts, and experiments exploiting X-ray microdiffraction to identify the order parameters and microstructure of these networks not only for the cuprates, but also for other complex superconductors, such as the pnictides for which analogous phase separation effects have been recently observed (63–65)

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